# **Data-Flow Analysis**

Data-flow analysis (DFA) provides information about how the **execution of a program may manipulate its data**.

Many different problems can be formulated as **data-flow problems**, for example:

- Which assignments to variable v may influence a use of v at a certain program position?
- Is a variable v used on any path from a program position p to the exit node?
- The values of which expressions are available at program position p?

Data-flow problems are stated in terms of

- · paths through the control-flow graph and
- properties of basic blocks.

Data-flow analysis provides information for global optimization.

# Data-flow analysis does not know

- which input values are provided at run-time,
- which branches are taken at run-time.

Its results are to be interpreted pessimistic

# Lecture Compilation Methods SS 2013 / Slide 218

## **Objectives**:

Goals and ability of data-flow analysis

# In the lecture:

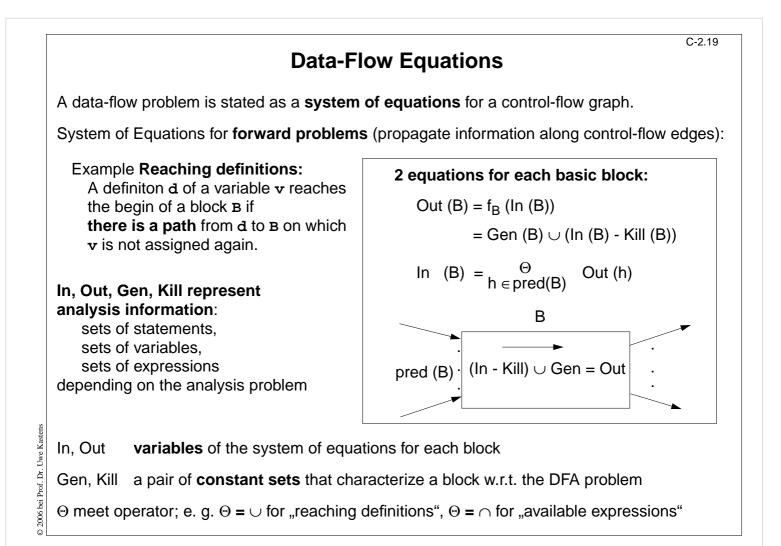
- Examples for the use of DFA information are given.
- Examples for pessimistic information are given.

## Suggested reading:

Kastens / Übersetzerbau, Section 8.2.4

# Questions:

- What's wrong about optimistic information?
- Why can pessimistic information be useful?



#### **Objectives**:

A DFA problem is modeled by a system of equations

#### In the lecture:

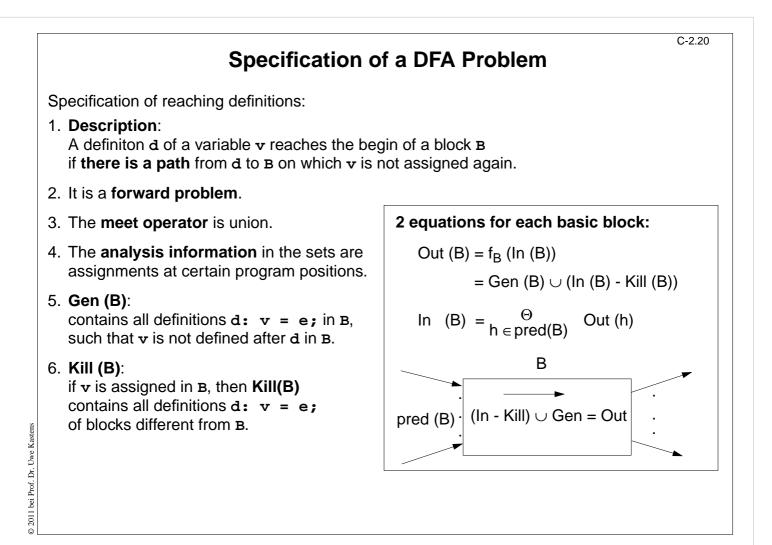
- The equation pattern is explained.
- Equations are defined over sets.
- In this example: sets of assignment statements at certain program positions.
- The meet operator being the union operator is correlated to "there is a path" in the problem statement.
- Note: In this context a "definition of a variable" means an "assignment of a variable".

### Suggested reading:

Kastens / Übersetzerbau, Section 8.2.4

#### **Questions:**

• Explain the meaning of In(B)= {d1: x=5, d4: x=7, d6: y=a+1} for a particular block B.



## **Objectives:**

Specify a DFA problem systematically

## In the lecture:

- The items that characterize a DFA problem are explained.
- The definition of Gen and Kill is explained.

#### Suggested reading:

Kastens / Übersetzerbau, Section 8.2.4

## **Questions:**

• Why does this definition of Gen and Kill serves the purpose of the description in the first item?

# Variants of DFA Problems

forward problem:
 DFA information flows along the control flow
 In(B) is determined by Out(h) of the predecessor blocks

**backward** problem (see C-2.23): DFA information flows **against the control flow** Out(B) is determined by In(h) of the successor blocks

 union problem: problem description: "there is a path"; meet operator is Θ = ∪ solution: minimal sets that solve the equations

**intersect** problem: problem description: "for all paths" meet operator is  $\Theta = \bigcirc$ solution: maximal sets that solve the equations

• optimization information: sets of certain statements, of variables, of expressions.

Further classes of DFA problems over general lattices instead of sets are not considered here.

Lecture Compilation Methods SS 2013 / Slide 221

## **Objectives:**

Summary of the DFA variants

## In the lecture:

• The variants of DFA problems are compared.

## Suggested reading:

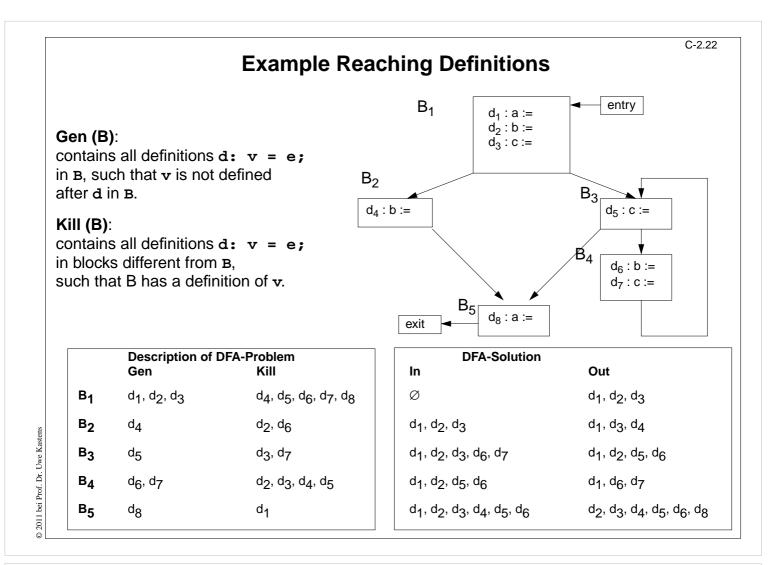
Kastens / Übersetzerbau, Section 8.2.4

## **Questions**:

• Explain the relation of the meet operator, the paths in the graph, and the maximal/minimal solutions.

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C-2.21



#### **Objectives**:

Understand the meaning of DFA sets

#### In the lecture:

• The example for C-2.20 is explained.

#### **Suggested reading:**

Kastens / Übersetzerbau, Section 8.2.4

#### **Questions:**

- Check that the In and Out sets solve the equations for the CFG.
- How can you argue that the solution is minimal?
- Add some elements to the solution such that it still solves the equations. Explain what such non-minimal solutions mean.

# **Iterative Solution of Data-Flow Equations**

Input: the CFG; the sets Gen(B) and Kill(B) for each basic block B Output: the sets In(B) and Out(B)

# Algorithm:

```
repeat
stable := true;
for all B ≠ entry {*}
do begin
   for all V ∈ pred(B) do
      In(B):= In(B) Θ Out(V);
   oldout:= Out(B);
   Out(B):= Gen(B) ∪ (In(B)-Kill(B));
   stable:= stable and Out(B)=oldout
  end
until stable
```

```
Initialization
Union: empty sets
for all B do
begin
    In(B):=Ø;
    Out(B):=Gen(B)
end;
```

### Intersect: full sets

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Complexity:  $O(n^3)$  with n number of basic blocks  $O(n^2)$  if  $|pred(B)| \le k \le n$  for all B

# Lecture Compilation Methods SS 2013 / Slide 222b

#### **Objectives**:

Understand the iterative DFA algorithm

## In the lecture:

The topics on the slide are explained. Examples are given.

- Initialization variants are explained.
- The algorithm is explained.

## Suggested reading:

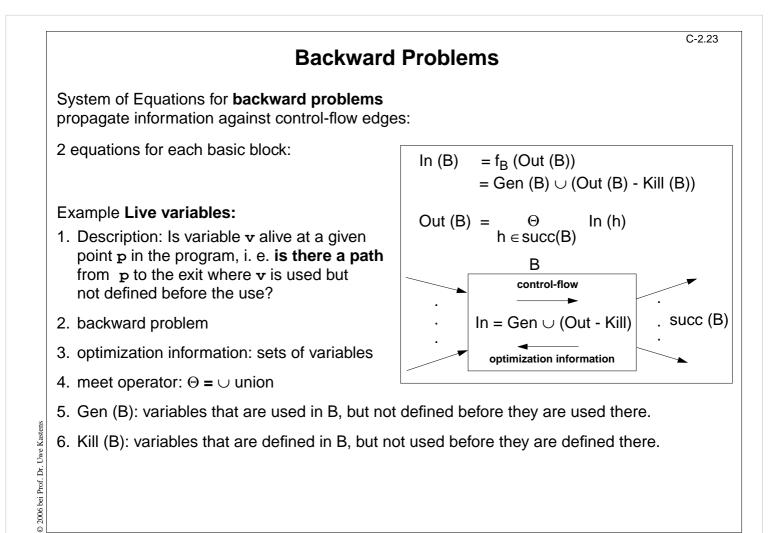
Kastens / Übersetzerbau, Section 8.2.5, 8.2.6

#### **Questions:**

• How is the initialization related to the size of the solution for the two variants union and intersect?

• Why does the algorithm terminate?

C-2.22b



## **Objectives:**

Symmetry of forward and backward schemes

## In the lecture:

The topics on the slide are explained. Examples are given.

- The equation pattern is explained.
- The DFA problem "live variables" is explained.

### Suggested reading:

Kastens / Übersetzerbau, Section 8.2.4

#### **Questions:**

• How do you determine the live variables within a basic block?

# Important Data-Flow Problems

- Reaching definitions: A definiton d of a variable v reaches the beginning of a block B if there is a path from d to B on which v is not assigned again.
   DFA variant: forward; union; set of assignments Transformations: use-def-chains, constant propagation, loop invariant computations
- Live variables: Is variable v alive at a given point p in the program, i. e. there is a path from p to the exit where v is used but not defined before the use.
   DFA variant: backward; union; set of variables
   Transformations: eliminate redundant assignments
- Available expressions: Is expression e computed on every path from the entry to a program position p and none of its variables is defined after the last computation before p. DFA variant: forward; intersect; set of expressions
   Transformations: eliminate redundant computations
- 4. Copy propagation: Is a copy assignment c: x = y redundant, i.e. on every path from c to a use of x there is no assignment to y?
  DFA variant: forward; intersect; set of copy assignments
  Transformations: remove copy assignments and rename use
- 5. Constant propagation: Has variable x at position p a known value, i.e. on every path from the entry to p the last definition of x is an assignment of the same known value. DFA variant: forward; combine function; vector of values Transformations: substitution of variable uses by constants

# Lecture Compilation Methods SS 2013 / Slide 224

# **Objectives:**

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Recognize the DFA problem scheme

# In the lecture:

- The DFA problems and their purpose are explained.
- The DFA classification is derived from the description.
- Examples are given.
- Problems like copy propagation oftem match to code that results from other optimizing transformations.

# Suggested reading:

Kastens / Übersetzerbau, Section 8.3

# Questions:

- Explain the classification of the DFA problems.
- Construct an example for each of the DFA problems.

# C-2.24a **Algebraic Foundation of DFA** DFA performs computations on a lattice (dt. Verband) of values, e. g. bit-vectors representing finite sets. It guarantees termination of computation and well-defined solutions. see [Muchnick, pp 223-228] A lattice L is a set of values with two operations: $\cap$ meet and $\cup$ join **Required properties:** 1. closure: x, y $\in$ L implies x $\cap$ y $\in$ L, x $\cup$ y $\in$ L 2. commutativity: $x \cap y = y \cap x$ and $x \cup y = y \cup x$ 3. associativity: $(x \cap y) \cap z = x \cap (y \cap z)$ and $(x \cup y) \cup z = x \cup (y \cup z)$ 4. absorption: $\mathbf{x} \cap (\mathbf{x} \cup \mathbf{y}) = \mathbf{x} = \mathbf{x} \cup (\mathbf{x} \cap \mathbf{y})$ 5. unique elements **bottom** $\perp$ , **top** T: $x \cap \bot = \bot$ and $x \cup T = T$ In most DFA problems only a **semilattice** is used with L, $\cap$ , $\perp$ or L, $\cup$ , T **Partial order** defined by meet, defined by join: $X \subseteq Y: X \cap Y = X$ $x \supseteq y: x \cup y = x$ (transitive, antisymmetric, reflexive)

# Lecture Compilation Methods SS 2013 / Slide 224a

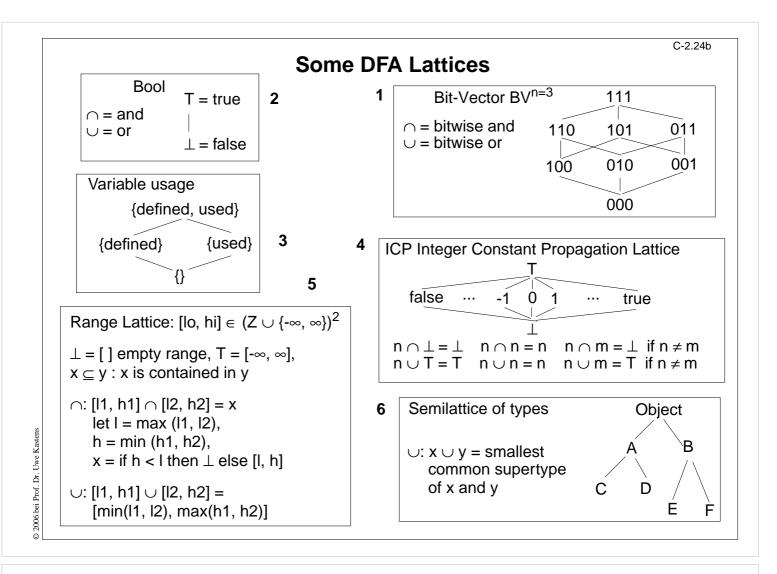
## **Objectives**:

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Recall algebraic structure lattice

#### In the lecture:

The topics on the slide are explained using examples of C-2.24b



#### **Objectives**:

Most important DFA lattices

## In the lecture:

- The Examples are explained.
- A new lattice can be constructed by elementwise composition of simpler lattices; e.g. a bit-vector lattice is an n-fold composition of the lattice Bool.
- A new lattice may be constructed for a particular DFA problem.

# C-2.24c Monotone Functions Over Lattices The effects of program constructs on DFA information are described by functions over a suitable lattice, e. g. the function for basic block B<sub>3</sub> on C-2.22: $\mathsf{f}_3(<\!\!x_1\ x_2\ x_3\ x_4\ x_5\ x_6\ x_7\ x_8\!\!>) = <\!\!x_1\ x_2\ 0\ x_4\ 1\ x_6\ 0\ x_8\!\!> \in\ \mathsf{BV}^8$ Gen-Kill pair encoded as function f: $L \rightarrow L$ is a **monotone function** over the lattice L if $\forall x, y \in L: x \subseteq y \Rightarrow f(x) \subseteq f(y)$ Finite height of the lattice and monotonicity of the functions guarantee termination of the algorithms. **Fixed points** z of the function f, with f(z) = z, is a solution of the set of DFA equations. MOP: Meet over all paths solution is desired, i. e. the "best" with respect to L MFP: Maximum fixed point is computed by algorithms, if functions are monotone If the functions f are additionally **distributive**, then **MFP = MOP**. f: $L \rightarrow L$ is a **distributive function** over the lattice L if $\forall x, y \in L: f(x \cap y) = f(x) \cap f(y)$

# Lecture Compilation Methods SS 2013 / Slide 224c

## **Objectives**:

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DFA equations and monotone functions

## In the lecture:

Understand solution of DFA equations as fixed point of monotone functions.

# Variants of DFA Algorithms

# Heuristic improvement:

Goal: propagate changes in the In and Out sets as fast as possible. Technique: visit CFG nodes in topological order in the outer for-loop {\*}. Then the number of iterations of the outer repeat-loop is only determined by back edges in the CFG

# Algorithm for backward problems:

Exchange In and Out sets symmetrically in the algorithm of C-2.22b. The nodes should be visited in topological order as if the directions of edges were flipped.

# Hierarchical algorithms, interval analysis:

Regions of the CFG are considered nodes of a CFG on a higher level. That abstraction is recursively applied until a single root node is reached. The Gen, Kill sets are combined in upward direction; the In, Out sets are refined downward.

# Lecture Compilation Methods SS 2013 / Slide 226

#### **Objectives:**

Overview on DFA algorithms

## In the lecture:

- The variants of the algorithm of C-2.25 are explained.
- The improvement is discussed.
- The idea of hierarchical approaches is explained.

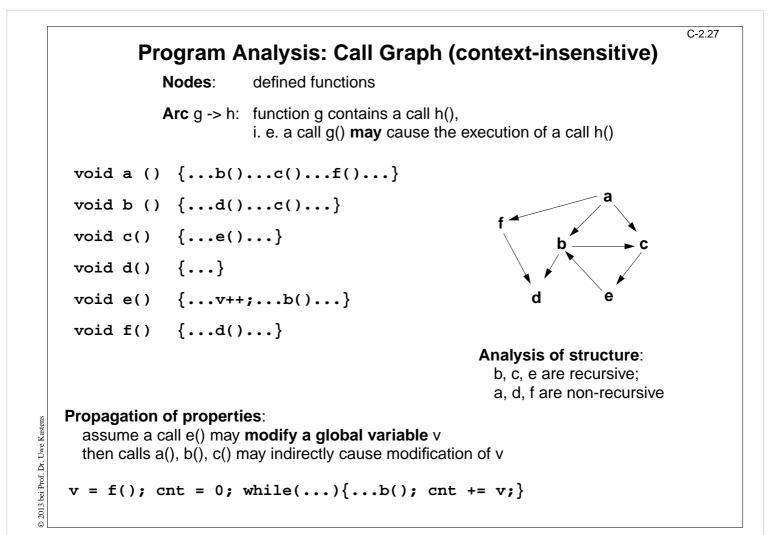
#### Suggested reading:

Kastens / Übersetzerbau, Section 8.2.5, 8.2.6

#### **Questions:**

• For a backward problem the blocks could be considered in reversed topological order. Why is that not a good idea?

C-2.26

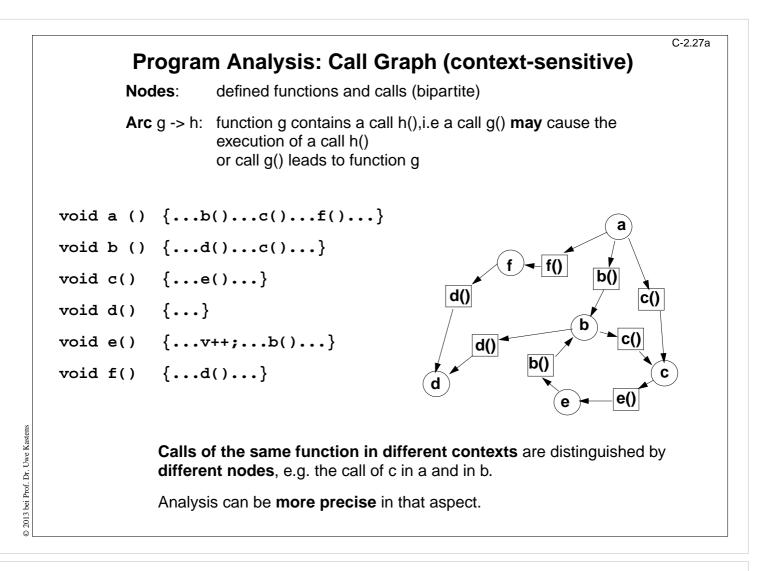


## **Objectives:**

Understand call graphs

## In the lecture:

- Structural abstraction of call relation,
- Structural properties, e. g. reachability,
- Simplified implementation of non-recursive functions, of functions without calls, of functions that are never called.
- Propagation of information along call paths.
- Description of function behaviour, e. g. no side-effect on global variables.

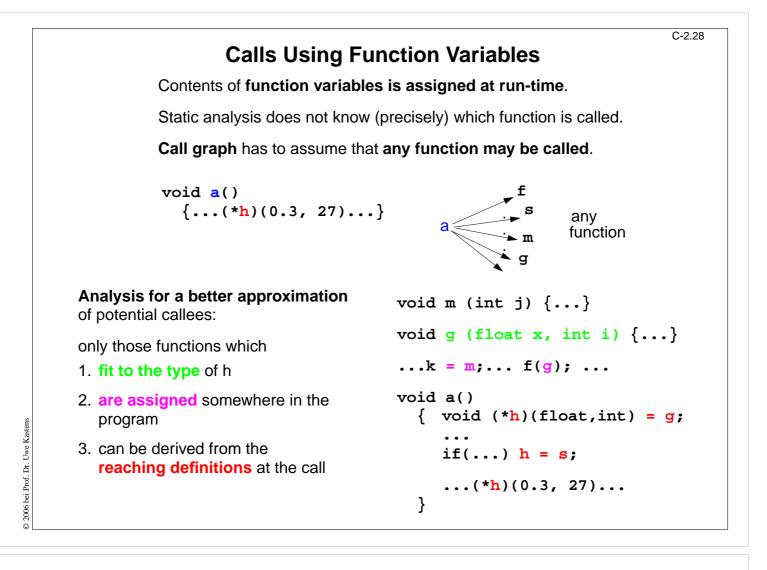


#### **Objectives:**

Understand context-sensitive call graphs

#### In the lecture:

Distinguish context-insensitive and context-sensitive call graphs

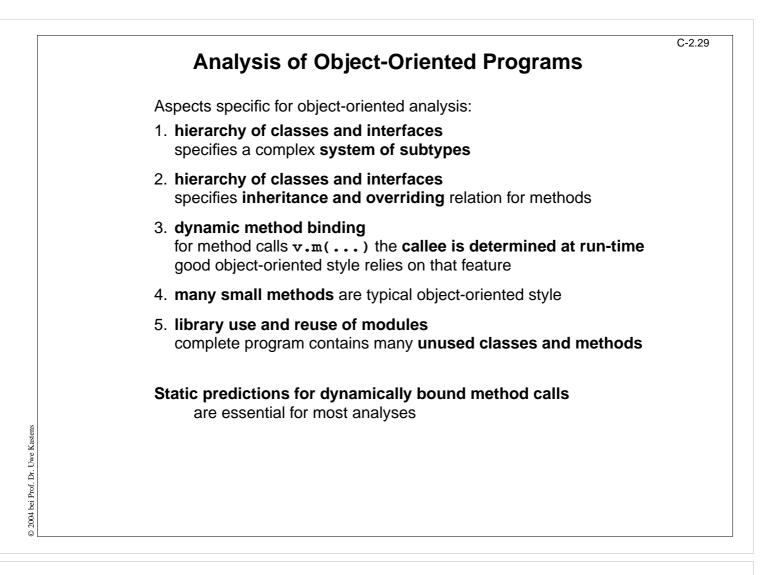


#### **Objectives**:

Approximate call targets

#### In the lecture:

- Explain the approximation techniques using the example.
- Relate the problem to dynamically bound method calls.

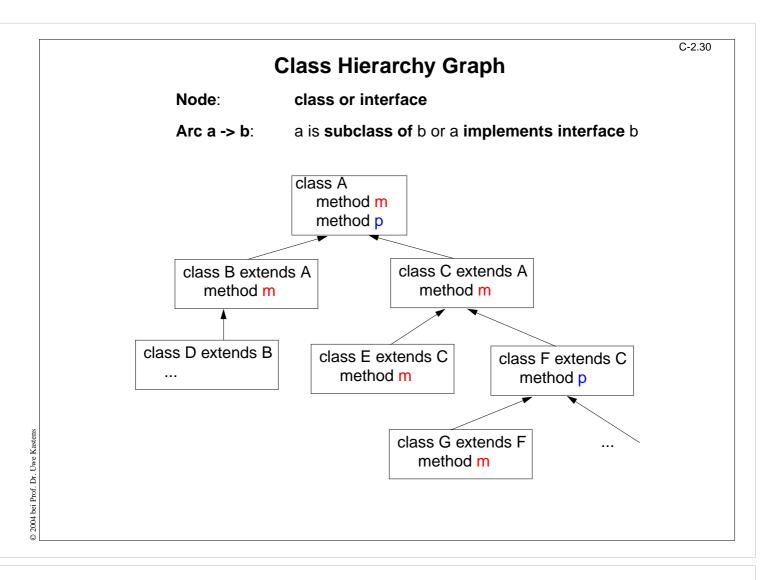


#### **Objectives**:

Overview on oo analysis issues

#### In the lecture:

- Role of class hierarchy for program analysis.
- Role of dynamic method binding for program analysis.



## **Objectives:**

Example for further consideration

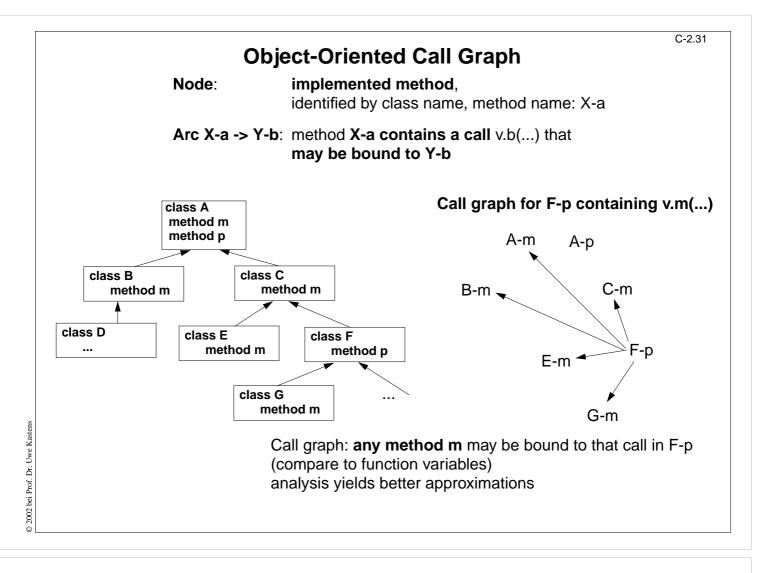
## In the lecture:

Recall central OO language properties:

- class hierarchy and typing,
- typed variables and method calls v.m(),
- inheritance of methods,
- overriding of methods,
- dynamically bound calls

# Assignments:

Recall the above mentioned language properties for Java and C++.

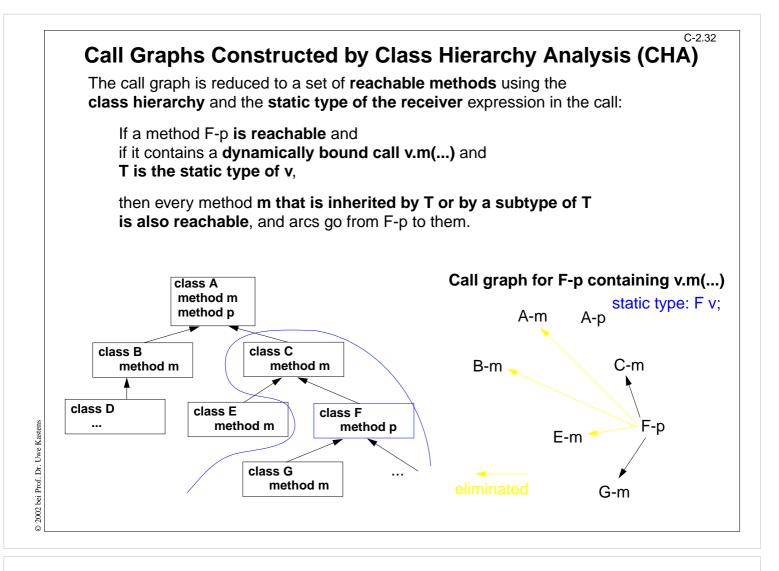


## **Objectives:**

Understand the call graph problem

#### In the lecture:

The topics on the slide are explained. using the example.



## **Objectives:**

## In the lecture:

The CHA method is explained using the example.

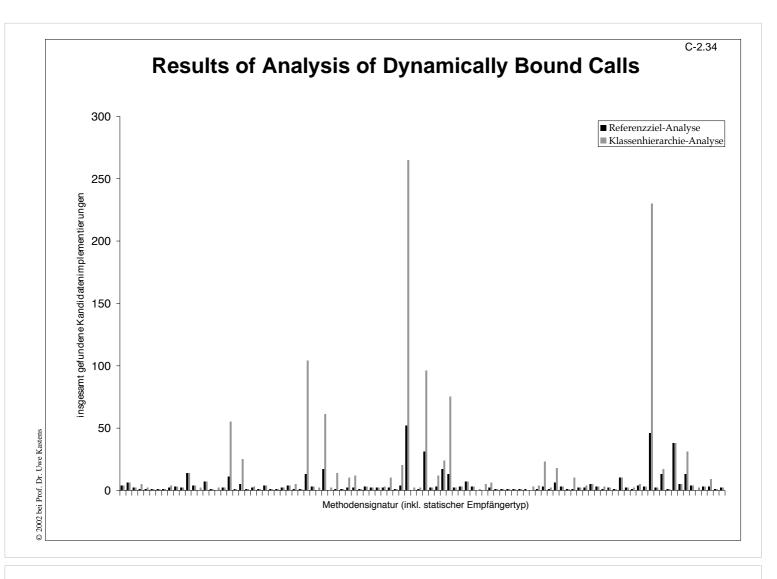
Refined Approximations for Call Graph Construction
Class Hierarchy Analysis (CHA): (see C-2.32)
Rapid Type Analysis (RTA):
As CHA, but only methods of those classes C are considered which are instantiated ( $new C()$ ) in a reachable method.
Reaching Type Analysis:
Approximations of run-time types is propagated through a graph: nodes represent variables, arcs represent copy assignments.
<b>Declared Type Analysis</b> : one node T represents all variables declared to have type T
Variable Type Analysis: one node V represents a single variable
Points-to Analysis:
Information on object identities is propagated through the control-flow graph

# **Objectives:**

Powerful OO type analyses

## In the lecture:

The methods are explained using small examples.



## **Objectives:**

Effects on call identification

## In the lecture:

The topics on the slide are explained. Examples are given.

- A pair of bars characterizes the number of method implementations, that may be bound to a set of calls having a particular type characteristics.
- Compare the results for CHA and points-to analysis.

# Modules of a Toolset for Program Analysis

analysis module	purpose	category	
ClassMemberVisibility	examines visibility levels of declarations	visualization	
MethodSizeStatistics	examines length of method implementations in bytecode operations and frequency of different bytecode operations		
ExternalEntities	histogram of references to program entities that reside outside a group of classes		
InheritanceBoundary	histogram of lowest superclass outside a group of classes		
SimpleSetterGetter	recognizes simple access methods with bytecode patterns		
MethodInspector	decomposes the raw bytecode array of a method implementation into a list of instruction objects	auxiliary analysis	
ControlFlow	builds a control flow graph for method implementations	- - fundamental analyses	
Dominator	constructs the dominator tree for a control flow graph		
Loop	uses the dominator tree to augment the control flow graph with loop and loop nesting information		
InstrDefUse	models operand accesses for each bytecode instruction		
LocalDefUse	builds intraprocedural def/use chains		
LifeSpan	analyzes lifeness of local variables and stack locations	1	
DefUseTypeInfo	infers type information for operand accesses	_	
Hierarchy	class hierarchy analysis based on a horizontal slice of the hierarchy		
PreciseCallGraph	builds call graph based on inferred type information, copes with incomplete class hierarchy	analysis of incomplete programs	
ParamEscape	transitively traces propagation of actual parameters in a method call (escape = leaves analyzed library)		
ReadWriteFields	transitive liveness and access analysis for instance fields accessed by a method call		

[Michael Thies: Combining Static Analysis of Java Libraries with Dynamic Optimization, Dissertation, Shaker Verlag, April 2001]

# Lecture Compilation Methods SS 2013 / Slide 235

## **Objectives**:

See analysis methods provided by a tool

#### In the lecture:

Some modules are related to methods presented in this lecture.

#### **Questions**:

Which modules implement a method that is presented in this lecture?