C-2.18

Data-flow analysis (DFA) provides information about how the **execution of a program may manipulate its data**.

Many different problems can be formulated as data-flow problems, for example:

- Which assignments to variable ${\bf v}$ may influence a use of ${\bf v}$ at a certain program position?
- Is a variable v used on any path from a program position p to the exit node?
- The values of which expressions are available at program position p?

Data-flow problems are stated in terms of

- paths through the control-flow graph and
- properties of basic blocks.

Data-flow analysis provides information for global optimization.

Data-flow analysis does not know

- which input values are provided at run-time,
- which branches are taken at run-time.

Its results are to be interpreted pessimistic

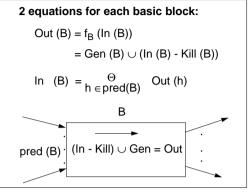
Data-Flow Equations

A data-flow problem is stated as a **system of equations** for a control-flow graph.

System of Equations for forward problems (propagate information along control-flow edges):

Example **Reaching definitions:** A definiton d of a variable \mathbf{v} reaches the begin of a block B if **there is a path** from d to B on which \mathbf{v} is not assigned again.

In, Out, Gen, Kill represent analysis information: sets of statements, sets of variables, sets of expressions depending on the analysis problem



In, Out variables of the system of equations for each block

Gen, Kill a pair of **constant sets** that characterize a block w.r.t. the DFA problem

 Θ meet operator; e. g. Θ = \cup for "reaching definitions", Θ = \cap for "available expressions"

Specification of a DFA Problem

Specification of reaching definitions:

1. Description:

A definiton d of a variable v reaches the begin of a block B if **there is a path** from d to B on which v is not assigned again.

- 2. It is a forward problem.
- 3. The meet operator is union.
- 4. The **analysis information** in the sets are assignments at certain program positions.
- 5. Gen (B): contains all definitions d: v = e; in B, such that v is not defined after d in B.
- 6. Kill (B):

if \mathbf{v} is assigned in \mathbf{B} , then **Kill(B)** contains all definitions $\mathbf{d}: \mathbf{v} = \mathbf{e}$; of blocks different from \mathbf{B} . 2 equations for each basic block: Out (B) = f_B (In (B)) = Gen (B) \cup (In (B) - Kill (B)) In (B) = $\bigoplus_{h \in pred(B)}^{\Theta}$ Out (h) B pred (B) $(\text{In - Kill}) \cup \text{Gen} = \text{Out}$

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Variants of DFA Problems

forward problem:

DFA information flows along the control flow In(B) is determined by Out(h) of the predecessor blocks

backward problem (see C-2.23): DFA information flows **against the control flow** Out(B) is determined by In(h) of the successor blocks

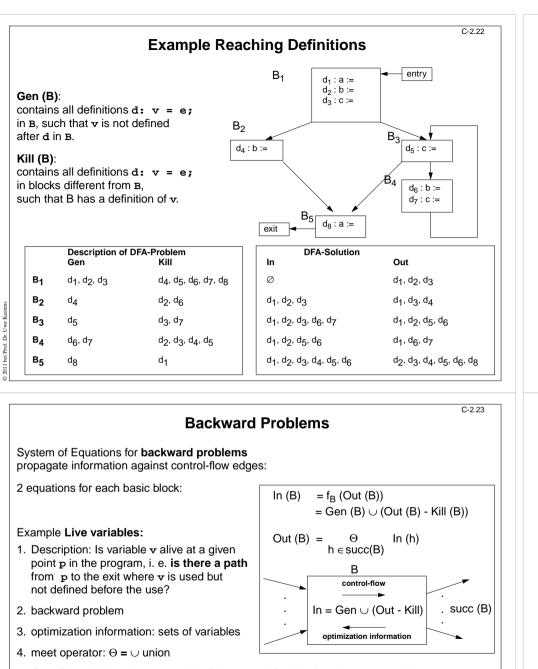
 union problem: problem description: "there is a path"; meet operator is Θ = ∪ solution: minimal sets that solve the equations

intersect problem: problem description: "for all paths" meet operator is $\Theta = \bigcirc$ solution: maximal sets that solve the equations

• optimization information: sets of certain statements, of variables, of expressions.

Further classes of DFA problems over general lattices instead of sets are not considered here.

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5. Gen (B): variables that are used in B, but not defined before they are used there.

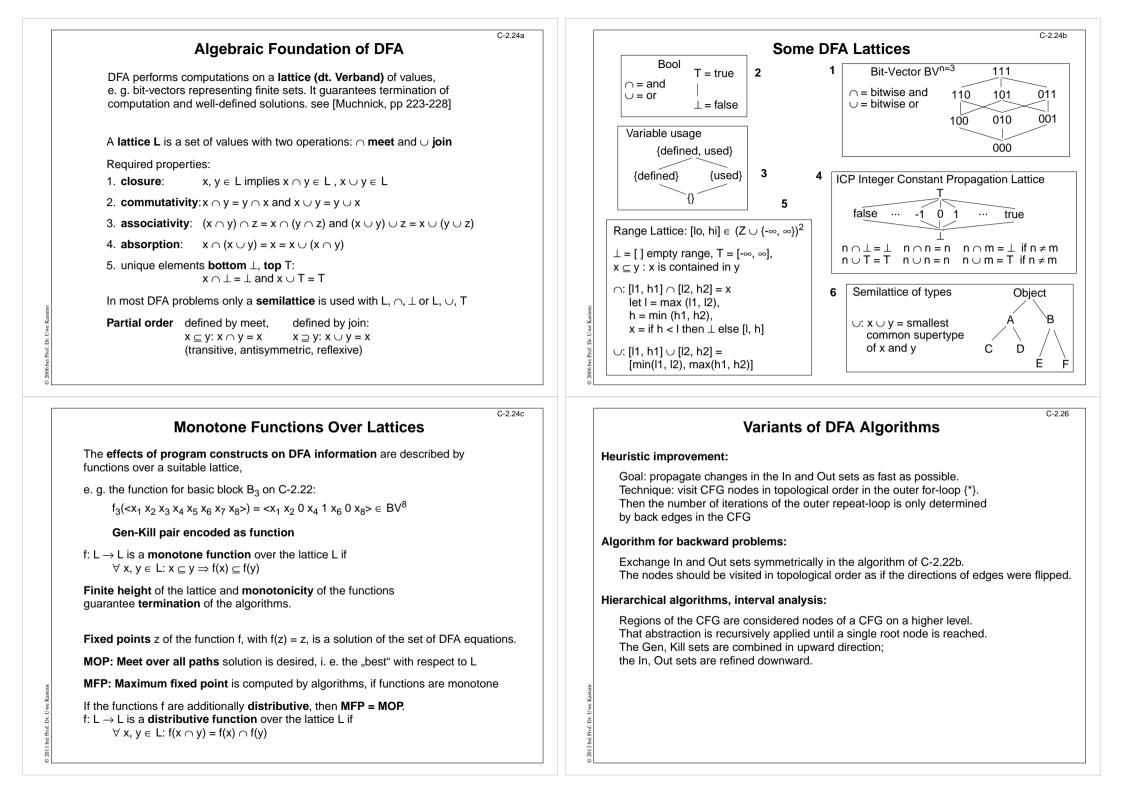
6. Kill (B): variables that are defined in B, but not used before they are defined there.

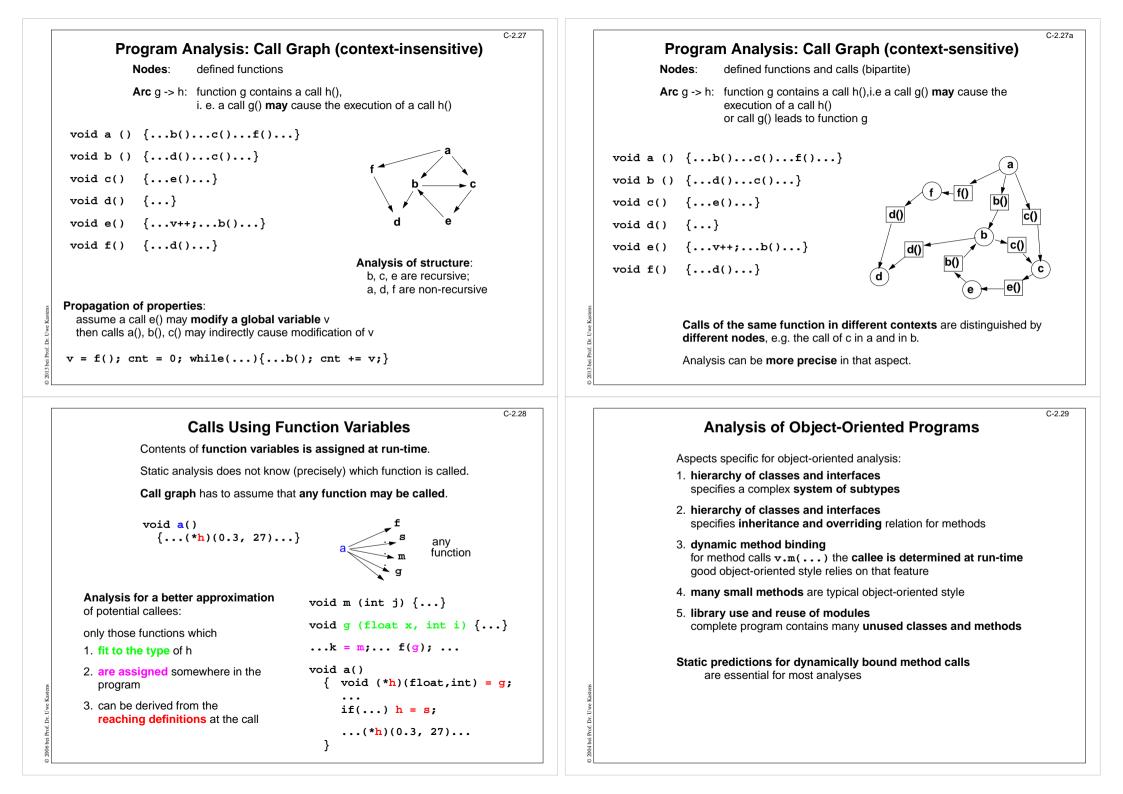
Iterative Solution of Data-Flow Equations

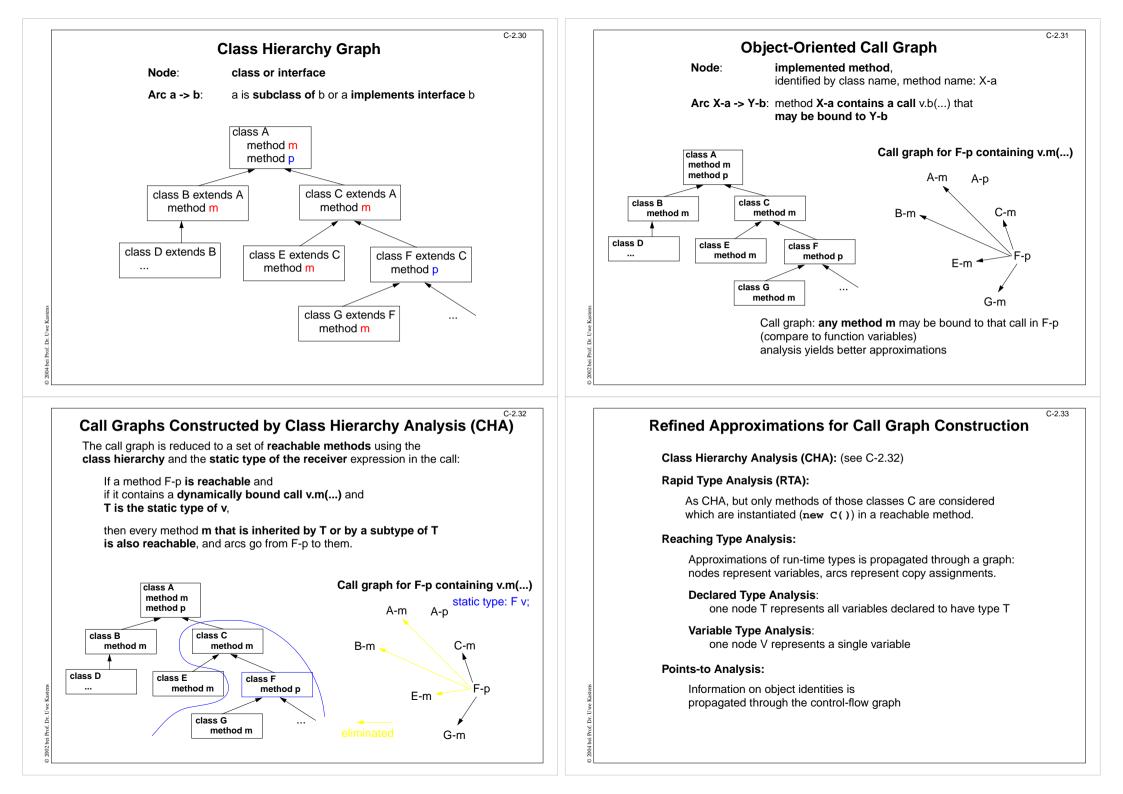
Input: the CFG; the sets Gen(B) and Kill(B) for each basic block B Output: the sets In(B) and Out(B)

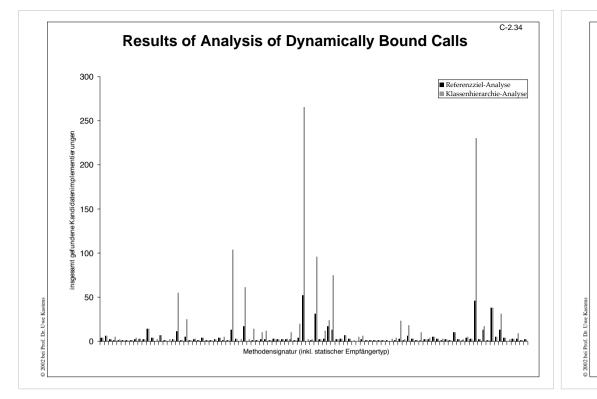
| Algorithm: | Initialization |
|--|---|
| <pre>repeat stable := true;</pre> | Union: empty sets |
| <pre>for all B ≠ entry {*} do begin for all V ∈ pred(B) do In(B):= In(B) Θ Out(V); oldout:= Out(B); Out(B):= Gen(B) ∪ (In(B)-Kill(B)); stable:= stable and Out(B)=oldout</pre> | <pre>for all B do begin In(B):=Ø; Out(B):=Gen(B) end; Intersect: full sets for all B do begin In(B) := U;</pre> |
| end until stable | Out(B):= Gen(B)U (U - Kill(B)) end; |

C-2.24 **Important Data-Flow Problems** 1. Reaching definitions: A definiton d of a variable v reaches the beginning of a block B if there is a path from d to B on which v is not assigned again. DFA variant: forward; union; set of assignments **Transformations:** use-def-chains, constant propagation, loop invariant computations 2. Live variables: Is variable \mathbf{v} alive at a given point \mathbf{p} in the program, i. e. there is a path from \mathbf{p} to the exit where \mathbf{v} is used but not defined before the use. DFA variant: backward; union; set of variables Transformations: eliminate redundant assignments 3. Available expressions: Is expression e computed on every path from the entry to a program position p and none of its variables is defined after the last computation before p. DFA variant: forward; intersect; set of expressions Transformations: eliminate redundant computations 4. Copy propagation: Is a copy assignment c: x = y redundant, i.e. on every path from c to a use of \mathbf{x} there is no assignment to \mathbf{y} ? **DFA variant:** forward: intersect: set of copy assignments **Transformations:** remove copy assignments and rename use **Constant propagation:** Has variable x at position p a known value, i.e. on every path from the entry to \mathbf{p} the last definition of \mathbf{x} is an assignment of the same known value. DFA variant: forward: combine function: vector of values Transformations: substitution of variable uses by constants









Modules of a Toolset for Program Analysis

| analysis module | purpose | category | |
|-----------------------|---|---------------------------------------|--|
| ClassMemberVisibility | examines visibility levels of declarations | visualization | |
| MethodSizeStatistics | examines length of method implementations in bytecode operations and frequency of different bytecode operations | | |
| ExternalEntities | histogram of references to program entities that reside outside a group of classes | | |
| InheritanceBoundary | histogram of lowest superclass outside a group of classes | | |
| SimpleSetterGetter | recognizes simple access methods with bytecode patterns | | |
| MethodInspector | decomposes the raw bytecode array of a method implementation into a list of instruction objects | auxiliary analysis | |
| ControlFlow | builds a control flow graph for method implementations | fundamental analyses | |
| Dominator | constructs the dominator tree for a control flow graph | | |
| Loop | uses the dominator tree to augment the control flow graph with loop and loop nesting information | | |
| InstrDefUse | models operand accesses for each bytecode instruction | | |
| LocalDefUse | builds intraprocedural def/use chains | | |
| LifeSpan | analyzes lifeness of local variables and stack locations | | |
| DefUseTypeInfo | infers type information for operand accesses | | |
| Hierarchy | class hierarchy analysis based on a horizontal slice of the hierarchy | analysis of incomplete programs | |
| PreciseCallGraph | builds call graph based on inferred type information, copes with incomplete class hierarchy | | |
| ParamEscape | transitively traces propagation of actual parameters in a method call (escape = leaves analyzed library) | | |
| ReadWriteFields | transitive liveness and access analysis for instance fields accessed by a method call | | |

[Michael Thies: Combining Static Analysis of Java Libraries with Dynamic Optimization, Dissertation, Shaker Verlag, April 2001]